

bezierplot

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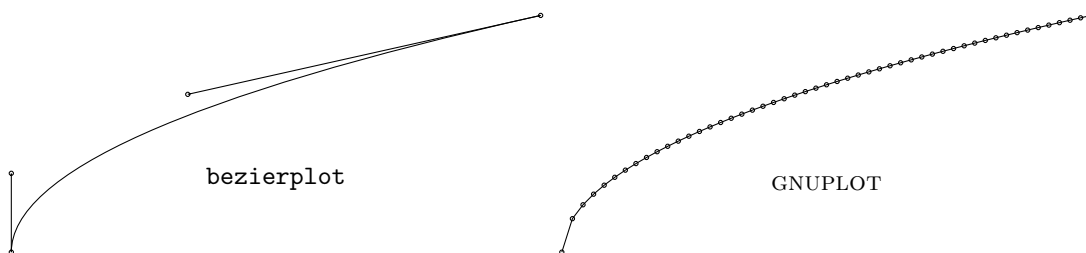
September 3, 2018

1 Introduction

`bezierplot` is a Lua program as well as a (Lua) \LaTeX package. This document describes both.

Given a smooth function, `bezierplot` returns a smooth bezier path written in `TikZ` notation (which also matches `METAPOST`) that approximates the graph of the function. For polynomial functions of degree ≤ 3 and inverses of them, the approximation is exact. `bezierplot` finds special graph points such as extreme points and inflection points and reduces the number of used points.

The following example will show a comparison of `GNUPLOT` with `bezierplot` for the function $y = \sqrt{x}$ for $0 \leq x \leq 5$:



`GNUPLOT` used 51 samples (no smoothing) and is still quite inexact at the beginning, whereas `bezierplot` uses 4 points only and is exact!

2 Installation

As `bezierplot` is written in Lua, the installation depends whether you are using `Lua\LaTeX` or another \LaTeX engine.

2.1 Installation For `Lua\LaTeX`

If you have installed `bezierplot` by a package manager, the installation is already complete. The manual installation of `bezierplot` is done in 2 steps:

- copy the files `bezierplot.lua` and `bezierplot.sty` somewhere in your `texmf` tree (e.g. to `~/texmf/tex/lualatex/bezierplot/bezierplot.sty` and `~/texmf/scripts/bezierplot/bezierplot.lua`)
- update the `ls-R` databases by running `mktexlsr`

2.2 Additional Installation Steps For Other \LaTeX Engines

You will have to call `bezierplot` as an external program via the option `--shell-escape` (`--write18` for `MiKTeX`). Therefore, `bezierplot.lua` has to be copied with the name `bezierplot` to a place, where your OS can find it. Under Linux this usually means copying to the directory `/usr/local/bin/`, but for Windows this will probably include more steps

(like adding to the `PATH`). Of course, Lua has to be installed as well. As soon as you can call `bezierplot` from a command line (e.g. by typing `bezierplot "x^2"`), it should also work with other \LaTeX engines.

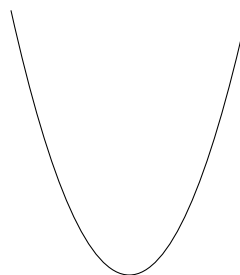
3 Loading

The `bezierplot` package is loaded with `\usepackage{bezierplot}`. There are no loading options for the package.

4 Usage

A minimal example of \LaTeX document could be:

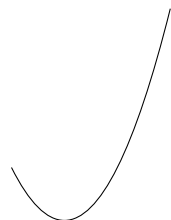
```
\documentclass{article}
\usepackage{tikz,bezierplot}
\begin{document}
\tikz \draw \bezierplot{x^2};
\end{document}
```



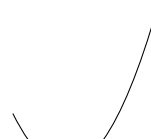
The command `\bezierplot` has 6 optional arguments in the sense of

`\bezierplot [XMIN] [XMAX] [YMIN] [YMAX] [SAMPLES] {FUNCTION}`

The defaults are `XMIN = YMIN = -5`, `XMAX = YMAX = 5` and `SAMPLES = 0` (this will set as few samples as possible).



`\bezierplot [-1] [2] {x^2}`



`\bezierplot [-1] [2] [0.5] [3] {x^2}`

You may reverse the graph by making `XMIN` bigger than `XMAX`. E.g.

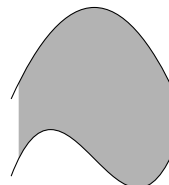
```
\bezierplot [-5] [5] {0.5*x+1}
```

returns $(-5, -1.5) \text{ -- } (5, 3.5)$, whereas

```
\bezierplot [5] [-5] {0.5*x+1}
```

returns the reversed path $(5, 3.5) \text{ -- } (-5, -1.5)$. This is useful, if you want to cycle a path to a closed area:

```
\begin{tikzpicture}
\fill[black!30] \bezierplot[-1] [1] {2-x^2}
-- \bezierplot[1] [-1] {x^3-x} -- cycle;
\draw \bezierplot[-1.1] [1.1] {2-x^2};
\draw \bezierplot[-1.1] [1.1] {x^3-x};
\end{tikzpicture}
```



4.1 Running Raw bezierplot

Of course, you can run `bezierplot.lua` in a terminal without using \LaTeX , e.g.

```
lua bezierplot.lua "3*x^0.8+2"
```

will return

```
(0,2) .. controls (0.03,2.282) and (0.268,3.244) .. (1,5)
```

You can set the window of the graph and the number of samples as follows:

```
lua bezierplot.lua "FUNCTION" XMIN XMAX YMIN YMAX SAMPLES
```

e.g.

```
lua bezierplot.lua "FUNCTION" 0 1 -3 2.5 201
```

will set $0 \leq x \leq 1$ and $-3 \leq y \leq 2.5$ and 201 equidistant samples. You may also omit the y -range, hence

```
lua bezierplot.lua "FUNCTION" 0 1
```

will set $0 \leq x \leq 1$ and leave the default $-5 \leq y \leq 5$. The variables `XMIN`, `XMAX`, `YMIN` and `YMAX` may also be computable expressions like `2*pi+6`:

```
lua bezierplot.lua "sin(x)" -pi pi
```

You may use `huge` for ∞ :

```
lua bezierplot "1/x" 0 1 0 huge
```

As `huge` is very huge and `bezierplot` uses recursive calls for nontrivial functions and non-fixed samples, this can last very long:

```
lua bezierplot "1/x" -5 5 -huge huge
```

But if you set fixed samples, it will be fast again (as this does not use recursive calls):

```
lua bezierplot "1/x" -5 5 -huge huge 100
```

4.2 Notation Of Functions

The function term given to `bezierplot` must contain at most one variable: x . E.g. `"2.3*(x-1)^2-3"`. You must not omit `*` operators:

wrong: $2x(x+1)$ correct: `2*x*(x+1)`

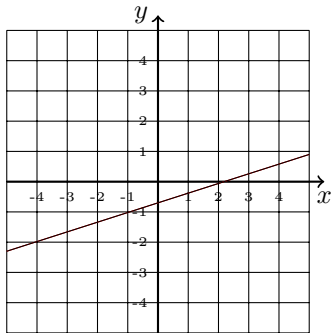
You have two possibilities to write powers: `"x^2"` and `"x**2"` both mean x^2 .

The following functions and constants are possible:

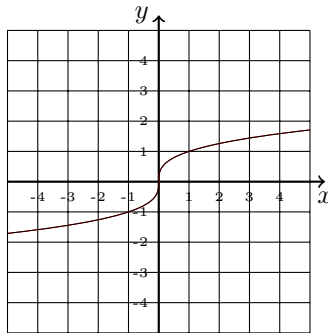
<code>abs</code>	absolute value (remember: your function should still be smooth)
<code>acos</code>	\cos^{-1} inverse function of cosine in radians
<code>asin</code>	\sin^{-1} inverse function of sine in radians
<code>atan</code>	\tan^{-1} inverse function of tangent in radians
<code>cbrt</code>	cube root $\sqrt[3]{\quad}$ that works for negative numbers, too
<code>cos</code>	cosine for angles in radians
<code>exp</code>	the exponential function $e^{(\quad)}$
<code>huge</code>	the numerical ∞
<code>e</code>	the euler constant $e = \exp(1)$
<code>log</code>	the natural logarithm $\log_e(\quad)$
<code>pi</code>	Archimedes constant $\pi \approx 3.14$
<code>sgn</code>	sign function
<code>sin</code>	sine for angles in radians
<code>sqrt</code>	square root $\sqrt{\quad}$
<code>tan</code>	tangent for angles in radians

5 Examples of bezierplot in Comparison with gnuplot

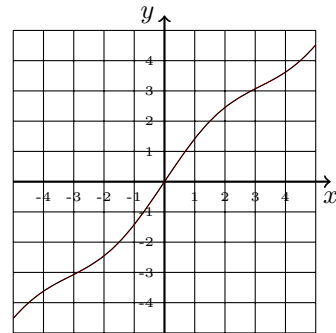
The following graphs are drawn with `bezierplot` (black) and `GNUPLOT` (red). `GNUPLOT` used 1000 samples per example. The functions are given below the pictures (left: `bezierplot`, right: `GNUPLOT`).



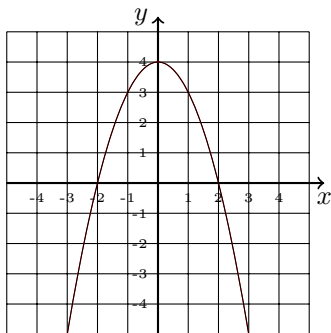
$0.32x-0.7$ | $0.32x-0.7$



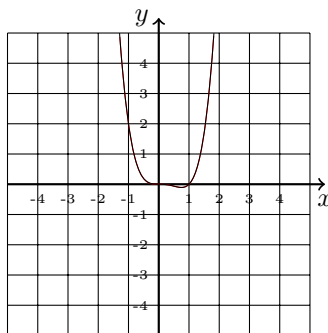
$\text{cbirt}(x)$ | $\text{sgn}(x) \cdot \text{abs}(x)^{(1/3.)}$



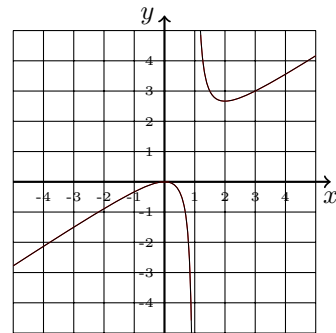
$x+0.5 \cdot \sin(x)$ | $x+0.5 \cdot \sin(x)$



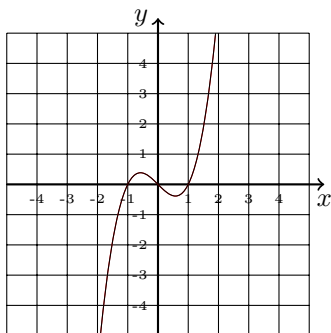
$-x^2+4$ | $-x^{**2}+4$



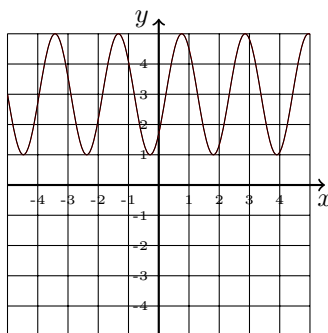
$x^3 \cdot (x-1)$ | $x^{**3} \cdot (x-1)$



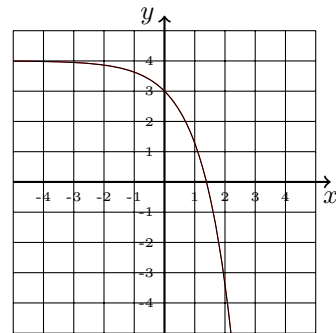
$2 \cdot x^2 / (3 \cdot x - 3)$ | $2 \cdot x^{**2} / (3 \cdot x - 3)$



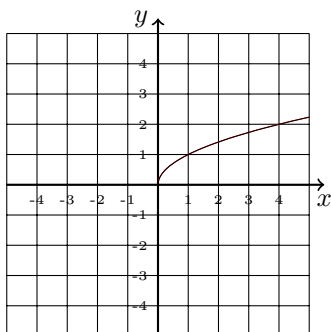
$(x+1) \cdot x \cdot (x-1)$ | $(x+1) \cdot x \cdot (x-1)$



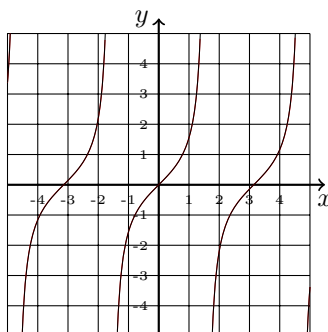
$2 \cdot \cos(3 \cdot x + 4) + 3$ | $2 \cdot \cos(3 \cdot x + 4) + 3$



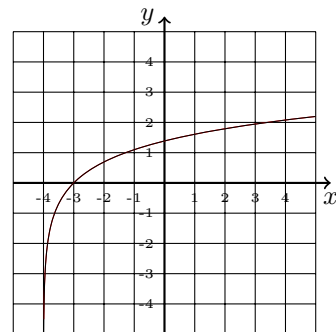
$4^{-\exp(x)}$ | $4^{-\exp(x)}$



$x^{0.5}$ | $x^{**0.5}$



$\tan(x)$ | $\tan(x)$



$\log(x+4)$ | $\log(x+4)$